Math 10 Quiz Chapter 13 and 12: ANOVA & Linear Correlation/Regression

Note: Our quiz solutions start on the third page of this document. The first two pages discuss the alligator data (which is real data).

The alligator data is a good example of why we can't predict for x values outside of the range of x values in our data.

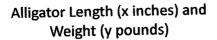
The 19 alligators in the quiz are a subsample of the sample that has 25 alligators. The 3 smallest and 3 largest alligators were removed from the original sample to create our subsample.

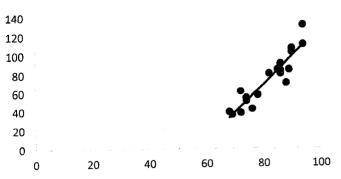
For the 19 alligators in our sample between 69 and 94 inches in length, the line DOES give a reasonable model to predict weight based on length.

However if we consider data outside that range, the linear relationship does not hold true. A curve would be a better fit.

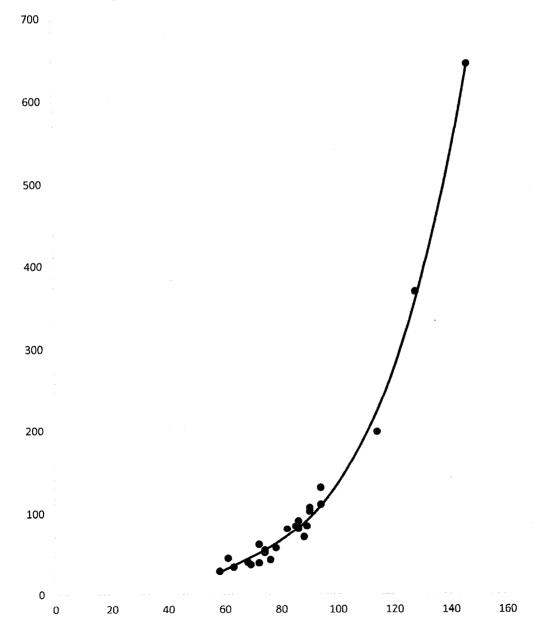
The next page contains a graph of a line fit to our subsample of 19 alligators' data and a curve fit to the entire sample of 25 alligators' data. You can see the curve is a better fit for the entire data set. The curve is a cubic curve (third degree). This makes sense as weight is better related to volume than to length.

The 128 inch alligator referred to in one of the quiz questions actually weighs 366 pounds but our line would have predicted its weight as only 211 pounds. That's why we should not predict outside the range of the x values in our data – we have no evidence to assume the linear relationship extends beyond our data, as it in fact does not in this particular data set.





Alligator length (x inches) and weight (y pounds)



Name Last First Cla Math 10 Quiz 7 Ch 12&13 Winter 2019 20 points	ss Time:	Yello	W (Not	orulette)
This quiz contains two questions, one question for analysis o regression and correlation.	f variance a	and one qu	estion for li	near
Question 1: 8 points; Environmental Studies	Lev	vel of Pollu	tant	
	Location	Location	Location	
The levels of a certain type of pollutant are monitored at three	A	В	C	
different monitoring sites: Location A, Location B, Location C.	8.2	7.9	8.5	
Data were collected for a random sample of 6 days at each	7.0	7.9	9.4	
location.		7.0	8.2	
Perform the appropriate hypothesis test to determine if the	7.8	 	7.6	
population average pollution levels are the same for all sites.	8.7	6.9	8.7	
On the board "use a = .05"	7.7	6.4		
	8.0	7.1	8.6	
For this sample data: $\overline{\overline{x}} = 7.833$	$\overline{x}_A = 7.9$	$\bar{x}_B = 7.1$	$\overline{x}_C = 8.5$	
Null Hypothesis: The population mean pollu				
all 3 locations are equal (MA				
Alternate Hypothesis: The population mean population			at-	
Some (or at least one) locations are	e differe	ent		
Test Statistic = 9.694 p-value = p-value = p-value? (Include degree braw the graph for this hypothesis test – label the test statistic on the graph for the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for this hypothesis test – label the test statistic on the graph for the grap				
Draw the graph for this hypothesis test materials to test successed on the gra	pii bilaac air	a moor mo p		
9,184 Test Stat	pvalue:	= <u>.</u> 002	•∞	alue La 02 6.05
Decision: Reject Ho				
Conclusion: At a 5% level of significa	nce w	e can		
conclude that the populat	ion Me	an pol	lution	
levels at some (or at least a				
locations are different from				
Note: If we had computer outported the differences between the med	ut to	anal	yze of that	-
The airferences				

KEY Yellow (No Form Letter

Question 2: 12 points: Environmental Studies

Biologists need to be able to estimate the weight of alligators in the wild, but weighing an alligator is a difficult and hazardous task. Length can be estimated from a photograph, which is much safer than trying to weigh an alligator.

So biologists would like a model that would allow them to estimate the weight of an alligator in the wild if they know its length. A regression line can be used to model the relationship between length and weight.

The data show lengths (in inches) and weights (in pounds) of a sample of 19 randomly selected alligators that were measured and weighed.

The calculator output is given to you. Use it!! (Do not put the data into your calculator.)

X=Length	94	74	86	86	86	94	69	72	85	82	88	72	74	90	89	68	76	90	78
Y=Weigh	130	51	80	90	83	110	36	38	84	80	70	61	54	106	84	39	42	102	57

a. [3 points] Find the correlation coefficient and write out the complete hypothesis test to determine whether it is significant.

Ho: P=0 HA: P +0 r=.93 pralue 4 a .000000008 4.05

Keject Ho

t=8.22 p=8.443E-9df=17 a=-168.8 b=2.97 s=10.27 $r^2=0.865$ r=0.93

Y=a+bx

 $\beta \neq 0$ and $\rho \neq 0$

b. [1 point] Prediction: Show work; round to values to 1 decimal place For an alligator that is 86 inches long, what is the weight predicted by the line?

$$\hat{y} = -168.8 + 2.97(86) = 86.6$$
 pounds

For a length of 82 inches: Find the residual (or "error") $y - \hat{y}$ d. [3 points] "Error Analysis":

Show work: round to values to 1 decimal place V =-168.8 +2.97(82) = 74.74 = 80-74.4 = 5.26

Is the observed data value above or below the best fit line? Above

Does the value predicted by the line overestimate or underestimate the observed (actual empirical) data value?

() nderestimate

e. [1 point] Prediction: Suppose that you were asked to use the line to predict weight for an alligator that is 128 inches in length. What should be your response?

We should not use the line to predict the weight of a 128 inch alligator. The length of 128 inches is not within the range of x values in the data (not between min and max x values induta)

f. [2 points] Interpretation of Slope: Write a sentence in the context of this situation that interprets (explains) what the slope of the best fit line tells us, and use its value in your interpretation.

For every I inch increase in length, an alliquious weight increases by 2.97 pounds, on average

g. [2 points] Interpretation of Coefficient of Determination: Write a sentence in the context of this situation that interprets (explains) what the Coefficient of Determination tells us for this problem, and use its value in your interpretation. Round to values to 1 decimal place as a percent (3 places in decimal form)

86,5% of the variation in weight can be explained